Fractal Geometry as an Effective Heat Sink

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“How long is the coast of Britain?” was the question stated by Mandelbrot. Using smaller and smaller rulers the coast length limits to infinity. If this logic is applied to the fractal heat sink geometry, infinite cooling capacity should be obtained using fractals with mathematically infinite surface area. The aim of this article is to check this idea using Richardson extrapolation of numerical simulation results varying the fractal element length from one to zero. As expected, the extrapolated cooling capacity has a noninfinite limit. The presented fractal heat sink geometry is non-competitive to the straight fins.

Keywords: fractal heat sink, light-emitting diode and central processing unit cooling, conjugate heat transfer, laminar flow, boundary element method, Koch snowflake

Highlights

- Infinite fractal heat transfer area leads to zero Nusselt number. Their product limits to finite value of heat flow.
- Richardson extrapolation of numerical simulation results confirm that.
- Fractal flow pattern follows fractal geometry.
- Fractal heat sink could not compete with straight fins.
- Conjugate heat transfer is simulated using boundary element method inhouse code.

0 INTRODUCTION

The convective heat transfer per unit time $\dot{Q}$ between a heat sink and the fluid is computed as

$$\dot{Q} = h A \Delta T,$$  \hspace{1cm} (1)

where $h$ is the heat transfer coefficient, $A$ the heat transfer area, and $\Delta T$ the temperature difference between the solid surface and fluid free stream. If the heat transfer area tends to infinity, the heat transfer power should tend to infinity too, presuming that the heat transfer coefficient and $\Delta T$ are finite nonzero values. The aim of this research is to test this assumption using computational fluid dynamics (CFD). The test is performed using a sequence of Koch snowflake fractal formation starting from a straight line to some small finite value, as shown in the last figure in the article. Using Richardson extrapolation [1], the results are extrapolated to the infinite surface area. If the result of this study confirms the idea, a very effective cooling device should be gained using fractal geometry.

The fractal geometry is encountered in nature in many shapes and purposes. For example, the blood veins with capillaries in lungs for heat and mass exchange. It is well known that the nature evolution solutions are superior to engineering ones in many areas. If this is true for heat sinks, then a fractal heat sink must exist to be better than simple one with the straight fins which is used nowadays in most cases. As it is a popular slogan: there is a room for improvement.

The geometry of heat sinks is subject of many recent articles [2–6]. The fractals are not an unknown topic in this subject. In most papers, fractal geometry is used to characterise the surface roughness [7], where the correlation between the critical heat flow and the fractal surface roughness of the pressure tubes from the cool heavy water moderator is investigated. A 3D laminar flow in a microchannel is analysed numerically in [8], where near wall swirls are obtained of size 1 $\mu$m. In the minority group of papers, fractal geometry is used to describe the material porosity, for example [9–12].

Elaborate review article of fractal heat exchangers is written in [13] where the list of similar articles is presented. Almost all of them are numerical simulations. The numerical feasibility study of fractal heat sink is published in [14], where fractal like heat sink is proposed for cooling of electronic device. The conjugate heat transfer in a fractal tree like channels network heat sink is studied numerically and experimentally [15]. A conclusion is made that a fractal heat sink has lower pressure drop, more uniform temperature field distribution, and higher coefficient of performance than that of the traditional helical channel net heat sink. In the latest review article [16] on optimization design of heat sinks the fractal geometry is mentioned only in one cited article [17]. A simple heat sink is simulated consisting of a fractal split microchannel up to second iteration formation only. The challenge of high cooling power in electronic devices and its dissipation using bionic Y-shaped
The geometry of the Koch snowflake represents the first cut out of the heat sink of the high heat density source, such as light-emitting diode (LED) or central processing unit (CPU) processor, as shown in Fig. 1. The bottom of the solid wall is heated to a constant temperature. The cooling fluid is flowing into the domain with constant velocity. The zero gradient outlet boundary condition is prescribed. It is not physically adequate since the flow field is not fully developed, but the obtained flow field is as expected at the outflow region and serves well for the numerical example aim. The buoyancy effect is neglected. This could be justified by small fluid solid temperature difference or orienting the gravity in the third dimension not influencing the flow field in the 2D computational cross-section shown in Fig. 1.

The problem is nondimensionalized as follows. Length quantities are nondimensionalized by the length of the computational domain in the mean flow direction. The velocity is nondimensionalized by the inlet velocity. The Reynolds number is computed as \( Re = \frac{Velocity@inlet \times Length}{v} \). The steady laminar flow of air is presumed as a cooling fluid. The Prandtl number is set to 0.71. The bottom dimensionless temperature is 1.0 and inlet temperature is zero. In this manner the temperature difference is defined to be 1 in Eq. (11). Computing the steady state solution, the fluid solid thermal diffusivity ratio is the last solution parameter investigated in next sections.

The non-dimensional form of governing equations for a 2D incompressible laminar flow are written using the nondimensional stream function vorticity formulation of Navier-Stokes equations. Stream function equation \( \psi \) is

\[
\frac{\partial^2 \psi}{\partial x^2} + \frac{\partial^2 \psi}{\partial y^2} = -\omega. \tag{2}
\]
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Inlet: \( \vec{v} = (1, 0), \) 
\( \psi = y, \) 
\( T = 0. \)

Interface:  
\( \vec{v} = (0, 0), \) 
\( \psi = 0, \frac{\partial \psi}{\partial n} = 0, \) 
\( T_s = T_f, \) 
\( k_s \frac{\partial T_s}{\partial n} = k_f \frac{\partial T_f}{\partial n}. \)

Lower wall: \( T = 1. \)

Outlet: 
\( \frac{\partial \psi}{\partial n} = 0, \) 
\( \frac{\partial T}{\partial n} = 0. \)

Left/Right solid wall: 
\( \frac{\partial T}{\partial n} = 0. \)

Free flow: \( \vec{v} = (1, 0), \) 
\( \psi = y, \frac{\partial \psi}{\partial n} = 1, \) 
\( T = 0. \)

Fluid: \( Re = \frac{1 \times \nu}{\nu}, \) 
\( Pr = \frac{\nu}{\alpha} = 0.71, \) 
\( k = \frac{k_s}{k_f}. \)

\[ \text{Fig. 1. The geometry of computational domain and boundary conditions} \]

**Table 2. Results sensitivity on solid fluid conductivity ratio \( k \) for \( Re = 1 \)**

<table>
<thead>
<tr>
<th>Solid fluid conductivity ratio ( k )</th>
<th>1</th>
<th>10</th>
<th>100</th>
<th>1000</th>
<th>10^4</th>
<th>10^5</th>
</tr>
</thead>
<tbody>
<tr>
<td>AVG (Interface temperature)</td>
<td>0.6529</td>
<td>0.9175</td>
<td>0.9900</td>
<td>0.9990</td>
<td>0.9999</td>
<td>1.0000</td>
</tr>
<tr>
<td>Change to prior - lower ( k ) [%]</td>
<td>-26.84</td>
<td>7.32</td>
<td>0.90</td>
<td>0.09</td>
<td>0.01</td>
<td></td>
</tr>
<tr>
<td>AVG (Outlet temperature)</td>
<td>0.4030</td>
<td>0.5236</td>
<td>0.5526</td>
<td>0.5562</td>
<td>0.5565</td>
<td>0.5565</td>
</tr>
<tr>
<td>Change to prior - lower ( k ) [%]</td>
<td>-23.03</td>
<td>5.25</td>
<td>0.65</td>
<td>0.05</td>
<td>0.00</td>
<td></td>
</tr>
<tr>
<td>AVG (Nusselt number)</td>
<td>0.5211</td>
<td>1.1167</td>
<td>1.3659</td>
<td>1.3994</td>
<td>1.4033</td>
<td>1.4036</td>
</tr>
<tr>
<td>Change to prior - lower ( k ) [%]</td>
<td>-53.33</td>
<td>18.25</td>
<td>2.39</td>
<td>0.28</td>
<td>0.02</td>
<td></td>
</tr>
<tr>
<td>Heat flow ( \dot{Q} ) [W]</td>
<td>0.0309</td>
<td>0.0663</td>
<td>0.0811</td>
<td>0.0831</td>
<td>0.0833</td>
<td>0.0833</td>
</tr>
<tr>
<td>Change to prior - lower ( k ) [%]</td>
<td>-53.33</td>
<td>18.25</td>
<td>2.39</td>
<td>0.28</td>
<td>0.02</td>
<td></td>
</tr>
<tr>
<td>Heat transfer coef. ( h ) [W/m²K]</td>
<td>0.0157</td>
<td>0.0172</td>
<td>0.0264</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>Change to prior - lower ( k ) [%]</td>
<td>-53.33</td>
<td>18.25</td>
<td>2.39</td>
<td>0.28</td>
<td>0.02</td>
<td></td>
</tr>
</tbody>
</table>

**Table 3. Results sensitivity on Reynolds number for \( k = 10 \)**

<table>
<thead>
<tr>
<th>Reynolds number ( Re )</th>
<th>1</th>
<th>10</th>
<th>100</th>
</tr>
</thead>
<tbody>
<tr>
<td>AVG (Interface vorticity)</td>
<td>-2.682</td>
<td>-2.777</td>
<td>-3.629</td>
</tr>
<tr>
<td>AVG (Interface temperature)</td>
<td>-0.9175</td>
<td>0.9054</td>
<td>0.8471</td>
</tr>
<tr>
<td>AVG (Outlet temperature)</td>
<td>0.3236</td>
<td>0.4766</td>
<td>0.3331</td>
</tr>
<tr>
<td>Nusselt number</td>
<td>1.1167</td>
<td>1.2231</td>
<td>1.7866</td>
</tr>
<tr>
<td>Heat flow ( \dot{Q} ) [W]</td>
<td>0.0063</td>
<td>0.0726</td>
<td>0.1031</td>
</tr>
<tr>
<td>Heat transfer coef. ( h ) [W/m²K]</td>
<td>0.0157</td>
<td>0.0172</td>
<td>0.0246</td>
</tr>
</tbody>
</table>

Vorticity equation \( \omega \) is
\[
\frac{\partial \omega}{\partial t} + \frac{\partial (v_x \omega)}{\partial x} + \frac{\partial (v_y \omega)}{\partial y} = \frac{1}{Re} \nabla^2 \omega \), \tag{3}
\]

where \( v_x = \frac{\partial \psi}{\partial y} \) and \( v_y = -\frac{\partial \psi}{\partial x} \). The energy equation within the fluid region is
\[
\frac{\partial T}{\partial t} + \frac{\partial (v_x T)}{\partial x} + \frac{\partial (v_y T)}{\partial y} = \frac{1}{Re Pr} \nabla^2 T \), \tag{4}
\]

where \( T \) is non-dimensional fluid temperature.

Energy equation within the solid region is
\[
\frac{\partial T}{\partial t} = \left( \frac{\alpha_s}{\alpha_f} \right) \frac{1}{Re Pr} \nabla^2 T \), \tag{5}
\]

where \( \alpha_s \) and \( \alpha_f \) are diffusivities for the solid and fluid regions respectively. For details on equations derivation [23]. The mechanism of heat conduction and its background is clearly explained in Liu et al. [9].

The interface boundary conditions on the wall between solid and fluid are written as temperature equality
\[
T_f = T_s \), \tag{6}
\]

and heat flux equality as
\[
k_f \left( \frac{\partial T}{\partial n} \right)_{f, \text{interface}} = -k_s \left( \frac{\partial T}{\partial n} \right)_{s, \text{interface}} \), \tag{7}
\]

where the \( n \) is unit normal direction to the fluid solid interface. The local Nusselt number is defined as the
Fig. 2. Meshes used; Increasing the mesh density the number of outlet nodes are 90, 180, 226 and 300 while on the shortest fractal element of the Koch boundary are 3, 3, 5 and 7 nodes

Table 4. Average values at the Koch fluid solid interface for fractal geometry sequence; the fractal element length is denoted using \( l \) and the complete interface length using \( L \); the Richardson extrapolation \cite{1} to infinite boundary is presented in the line \( l = 0 \) including extrapolation accuracy estimation interval. In the last line, the best guestimate values are stated

<table>
<thead>
<tr>
<th>( l )</th>
<th>( L )</th>
<th>( \omega_{Koch} )</th>
<th>( T_{Koch} )</th>
<th>( Nu )</th>
<th>( \dot{Q} )</th>
<th>( h )</th>
</tr>
</thead>
<tbody>
<tr>
<td>1.000</td>
<td>1.000</td>
<td>-18.58</td>
<td>0.9999</td>
<td>8.158</td>
<td>0.1149</td>
<td>0.1149</td>
</tr>
<tr>
<td>0.333</td>
<td>1.333</td>
<td>-15.52</td>
<td>0.9998</td>
<td>6.071</td>
<td>0.1140</td>
<td>0.0855</td>
</tr>
<tr>
<td>0.111</td>
<td>1.778</td>
<td>-8.958</td>
<td>0.9998</td>
<td>4.980</td>
<td>0.1247</td>
<td>0.0701</td>
</tr>
<tr>
<td>0.037</td>
<td>2.370</td>
<td>-6.397</td>
<td>0.9998</td>
<td>3.954</td>
<td>0.1320</td>
<td>0.0557</td>
</tr>
<tr>
<td>0.012</td>
<td>3.160</td>
<td>-4.578</td>
<td>0.9998</td>
<td>3.051</td>
<td>0.1358</td>
<td>0.0430</td>
</tr>
<tr>
<td>0.004</td>
<td>4.214</td>
<td>-3.629</td>
<td>0.9998</td>
<td>2.332</td>
<td>0.1384</td>
<td>0.0328</td>
</tr>
<tr>
<td>0.0</td>
<td>( \infty )</td>
<td>-2.518</td>
<td>0.9998</td>
<td>2.332</td>
<td>0.1384</td>
<td>0.0328</td>
</tr>
<tr>
<td>acc. est. ±</td>
<td>1.0</td>
<td>0.0000</td>
<td>1.6</td>
<td>0.0081</td>
<td>0.0219</td>
<td></td>
</tr>
<tr>
<td>guestimate</td>
<td>-2.518</td>
<td>0.9998</td>
<td>0</td>
<td>0.1446</td>
<td>0</td>
<td></td>
</tr>
</tbody>
</table>

The average Nusselt number \( Nu \) is the integral value computed as

\[
Nu = \frac{1}{L} \int_0^L Nu \, dl ,
\]

where \( L \) is the interface wall length. The heat flow \( \dot{Q} \) is computed using its definition as

\[
\dot{Q} = -A k_f \left( \frac{\partial T}{\partial n} \right)_f = (L \cdot 1) k_f Nu ,
\]

where \( A \) is the actual interface area computed as \( L \cdot 1 \). The unity length is defined on the 3rd dimension. Heat transfer coefficient \( h \) is computed as

\[
h = \frac{\dot{Q}}{A \Delta T}
\]

where \( \Delta T \) is one in this case.

In this paper only a steady solution is computed. The steady solution is solid thermal diffusivity \( \alpha_s \) independent since the time derivative is zero, see Eq. (5). In this manner the solid fluid thermal conductivity ratio \( k \) defined as \( k = k_s/k_f \) is the only solid material temperature derivative at the fluid side of the fluid solid interface as

\[
Nu = - \left. \frac{\partial T}{\partial n} \right|_{f, \text{interface}} .
\]
2 RESULTS AND DISCUSSION

The basic aim of the article is to check the assumption about the infinite heat flow for infinite length of fractal solid-fluid interface. Before this main numerical test, a few necessary tests are performed using the finest fractal geometry which is numerically the most cumbersome to solve.

2.1 Mesh Sensitivity Study

The aim of this test is to choose the appropriate mesh density and numerical solution accuracy estimation using standard procedure described in [1]. Four mesh densities were used: coarse, medium, fine and finest, see Fig. 2. In Tab. 1 the results are shown for the selected case $Re = 1$ and solid fluid conductivity ratio $k = 1$.

Three integral values are selected as numerical solution accuracy indicators: average (AVG) value of vorticity, temperature and Nusselt value on the solid fluid interface. The AVG (Interface vorticity)
numerical solution accuracy is the worst among all, being 0.50%, which is to be expected since the interface vorticity is the most nonlinear and therefore difficult to solve. The thermal solutions are less mesh sensitive, resulting in maximal 0.02% error for average temperatures and 0.16% error for the Nusselt number. Obviously and intuitively, the temperature profile over the interface is less mesh dependent than the vorticity one. Based on the CPU consumption and basic aim, the fine mesh was chosen as a default mesh for all further computations resulting in less than 1% numerical solution accuracy. Similar numerical accuracy is published in the work [23] where using the same BEM code the benchmark conjugate heat transfer problem was solved.

2.2 Reynolds Number Dependency of Isothermal Solution

The contour plots are presented in Figs. 3 and 3 for stream function and vorticity field at $Re = 1$ and $Re = 100$. Close to the Koch snowflake boundary, the streamlines in Figs. 3 are almost symmetrical with respect to the upstream and downstream sides for $Re = 1$. For a higher $Re$ number the symmetry feature is altered, since the recirculation zone appears. In contrast to $Re = 1$, in general, the bright blue colour representing positive stream value change to dark blue colour representing negative stream value on the downstream side. The dark blue zones represent the clockwise and light blue counter clockwise rotation vortices. The symmetry issues are more evident in the smallest cavities. This feature is also visible on vorticity contour plots as a dark and bright red colour, representing the zero-value vorticity contour.

The flow self-similarity is discussed in the next paragraph. Streamlines are shown in Fig. 4, where two successive zooms are enlarged on the right-hand side of the full-scale plot. Zooms 1 and 2 were selected in such a manner that the geometric self-similarity is evident. The flow pattern self-similarity is obvious too, especially for $Re = 1$. The flow pattern is discussed in many aspects in our latest work completely dedicated to the isothermal solution [25].

2.3 Influence of Solid Fluid Conductivity Ratio $k$

The real solid fluid conductivity ratio $k$ values are 16000, 9000 and 2300 for Cu, Al and steel heat sink material, respectively. The test values are chosen to be in the range from 1 to $10^5$. The Nusselt...
values are not changing significantly (only 2.39 %) when increasing \( k \) over 100, see Tab. 2 and Fig. 5, indicating no significant changes. Increasing \( k \), solid gradients decrease obtaining an almost constant solid temperature. Replacing the steel with Al the cooling heat flow increases for 0.3 % in this problem configuration. The neglecting improvement of 0.02 % is obtained replacing Al with Cu.

Interesting temperature contours are obtained for \( k = 1 \), equalling the heat conductivity in fluid and solid, see Fig. 5. In this case (\( Re = 1 \)), the solid domain influence on temperature nearly vanishes, since the conduction equals convection, obtaining large temperature gradients in the solid domain.

The Biot number (\( Bi = Length \cdot h/k_s \)) analysis follows. The characteristic \( Length \) is defined in this case as \( Length = A/L \) where the \( A \) is finite heat sink cross section approximately 0.1 \( \cdot 1 \) and \( L \) the length of the fractal cooling surface area. Increasing \( L \) to the infinity the characteristic length and \( Bi \) limits to zero. Additionally, increasing \( k \) and consequently \( k_s \) values the \( Bi \) number also limits to zero value. Both parameters clearly indicating very low \( Bi \) values and consequently the uniform solid temperature as already mentioned. Using results in Tab. 2 the maximum \( Bi \) number value is \( Bi = 0.0002 \) using \( L = 4.214 \), \( Length = 0.0237 \), \( h = 0.0073 \) and \( k = 1 \), confirming that heat conduction in solid prevails heat convection to fluid.

### 2.4 Influence of Reynolds Number on the Thermal Solution

For this test, the fluid solid conductivity ratio \( k \) value is fixed to 10 in order to obtain temperature changes in the solid. In this academic case the heat sink is made using isolative material such as wood or plastic. Increasing the \( Re \) number, the heat convection prevails over diffusion, resulting in nearly linear growth of the Nusselt number values, see Tab. 3 and Fig. 6. One should expect that increasing \( Re \) and consequently the cooling heat rate, the outlet temperature should increase too. Wrong, the outlet temperature decreases since the mass flow
increases. The proper thermodynamic conclusion in this case would be: the enthalpy of outflow, computed as mass flow and temperature product, increases and exergy decreases. Increasing \( Re \) number the interface temperature decreases too, indicating higher temperature gradients and consequently, higher heat flux in the solid domain.

### 2.5 The Infinite Heat Flow Idea

The infinite heat flow idea is tested by forming Koch snowflake fractal geometry starting from the flat heat sink geometry denoted by \( l = 1 \), where \( l \) is the fractal element length. The next geometry iteration is obtained by dividing each fractal element by factor 3 and creating 4 new elements using the Koch snowflake formation procedure, see Fig. 8. In this manner, the Koch boundary length is increased by factor \( 4/3 \) at each formation iteration giving an infinite limit. The final boundary length in this research is \((4/3)^5 = 4.214\) using 5th iteration formation and fractal element size \( l = (1/3)^5 = 0.004\). Using Richardson extrapolation [1], the numerical result values limit is computed using \( l \) as mesh size parameter which tends to zero. The accuracy estimation is also a part of the extrapolation procedure results.

The infinite heat flow assumption is tested using \( Re = 100 \) and solid fluid conductivity ratio \( k = 10^4 \) which matches the Aluminium heat sink material approximately.

In the Figs. 8, 9 and 10 the contour plots of stream function, vorticity and temperature are plotted respectively for each fractal element length \( l \). It is interesting and natural to expect that the flow fields have the same fractal nature as the geometry has in the Koch snowflake formation procedure. This is more evident in the upwind side of the heat sink in comparison to the downwind side where the recirculation zone is present.

The quantitative results are presented in Tab. 4 and graphically in Fig. 7. Observing the heat flow \( \dot{Q} \) dynamics the smooth response is obtained generally. The only exception is in the first iteration between \( l = 1.0 \) and \( l = 0.333 \). The first question would be how it is possible, that the cooling heat flow is slightly lower for 0.8 % using a single rib (\( l = 0.333 \)) comparing to the flat surface (\( l = 1.0 \)). While the surface area

![Graphical presentation of tabulated results in Tab. 4; the shaded area is accuracy estimation of extrapolated result value computed using [1](image)](image)
of ribbed surface $A$ is increased, the heat transfer coefficient $h$ is significantly decreased resulting in slightly lower heat flow which is their product $\dot{Q} = h \cdot A \cdot \Delta T$. In this case the cooling rib is more of a fluid flow and thermal obstacle than cooling enhanced as expected intuitively. Additionally, the recirculation zone performs thermal isolation increasing the thermal boundary layer thickness in downwind area comparing to the flat surface case, see Fig. 10.

The next objectivity of discussion is to verify that the five iterations of the Koch snowflake formation are enough for the testing aim. Comparing results in the last two figures, namely $l = 0.012$ and $l = 0.004$, the macro flow solution does not change any more significantly. Decreasing $l$ further approaching the roughness size value, the flow would change only very close to the boundary until the viscous forces would damp the smallest swirls in cavities limiting to the hydraulic smooth surface flow. If the dimension of the heat sink would be 1 cm, then the shortest fractal element length $l = 0.004$ would be $40 \, \mu m$, which is equivalent to the N11 Roughness Grade Number which is obtained using sand cast or hot roll manufacturing of heat sink, [26]. Finally, the minimal edge dimension of $l = 40 \, \mu m$ is still big enough to be in the continuum mechanics having a Knudsen number value of 600.

3 CONCLUSIONS

The infinite cooling capacity idea is very naive. The numerical experiment annulated the idea of course. Decreasing the fractal length $l$ to zero the main conclusions are:

- The area of interface surface converges to infinity.
- $Nu$ and $h$ converged to zero setting the convective heat flow to zero (bearing in mind the extrapolation error).
- The $\dot{Q}$ is increasing monotonically to a specific finite value: heat diffusion.
2 and 4 indicating the optimal fin should be slenderer generating larger temperature changes. This is clearly revealed by almost constant fractal fin heat sink? No. This kind of fractal heat sink is at the fluid solid interface. The numerical experiment solid surface to fluid is achieved by heat diffusion only that each real surface has a roughness, might be in the fractal manner or not, and that the heat convection from solid surface to fluid is achieved by heat diffusion only at the fluid solid interface. The numerical experiment in this article confirms this fact.

The fractal geometry heat sink as an effective heat sink? No. This kind of fractal heat sink is non-competitive to the simple straight fin heat sink. This is clearly revealed by almost constant fractal fin temperature for aluminium – air configuration in Tab. 2 and 4 indicating the optimal fin should be slenderer generating larger temperature changes.

In this manner the resulting heat transfer Eq. (11) could be written as

\[
\dot{Q} = \lim_{l \to 0} \left( (h \to 0)(A \to \infty)(\Delta T = 1) \right) 
\]

as stated in Eq. (10). Since the Nusselt number represents the ratio between convection and diffusion, setting the \( Nu \to 0 \) annulated heat convection leaving the diffusion the only heat transfer mechanism in the solid fluid interface, as it is the fact. The fact is also, that each real surface has a roughness, might be in the fractal manner or not, and that the heat convection from solid surface to fluid is achieved by heat diffusion only at the fluid solid interface. The numerical experiment in this article confirms this fact.

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5 REFERENCES


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