

Thermally Induced Dynamics of an Aero-Engine Active Magnetic Bearing–Rotor System

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Abstract Under high-temperature operating conditions in aero-engines, the combined effects of nonuniform heat generation in active magnetic bearing (AMB) coils and ambient thermal loads can lead to nonuniform temperature distributions within the rotor system, thereby generating thermal bending loads and degrading the system's dynamic stability. To address this issue, a one-way sequential thermo-mechanical analysis framework for an AMB-supported rotor system is developed. The model incorporates thermally induced loads derived from the temperature field, disk unbalance, gravity, and the PID-dependent equivalent stiffness and damping of the AMBs. The governing equations are solved using the Newmark- β method. Based on the proposed model, the dynamic response characteristics of the system under varying bias currents, rotational speeds, and ambient temperatures are systematically investigated. The results show that, under a given thermal condition, increasing the bias current enhances the effective support capability of the AMB, thereby reducing the vibration response. In contrast, increasing the rotational speed progressively amplifies the synchronous vibration response, with a more pronounced increase near the upper end of the investigated speed range. Furthermore, increasing the ambient temperature significantly increases the thermally induced bending excitation, resulting in larger vibration amplitudes. This suggests that, within the investigated operating range, thermal effects strongly affect the system's dynamic behavior. This study provides a theoretical basis for thermal stability assessment and vibration control of AMB-supported rotor systems operating under high-temperature conditions.

Keywords thermally induced vibration, active magnetic bearing, aero-engine, rotor dynamics

Highlights

- Increasing the bias current reduces the displacement amplitude and contracts the shaft orbit without altering the response periodicity.
- Increasing the rotational speed amplifies the synchronous vibration response, particularly in the upper portion of the investigated speed range.
- Thermal bending moments cause pronounced shaft-orbit center migration while the response remains dominated by the fundamental-frequency component.

1 INTRODUCTION

Magnetic bearings offer frictionless high-speed operation, high efficiency, low energy consumption, and active controllability, making them a promising support technology for aero-engines and steam turbines [1]. To further investigate the coupled dynamic behavior of magnetic bearing–rotor systems, researchers have developed various high-precision dynamic models based on their electromagnetic properties, control logic, and dynamic response. These modeling approaches have been integrated with rotor-dynamics theory, enabling systematic investigation of the dynamic behavior of magnetic-bearing–rotor systems [2, 3]. Gao et al. [4] investigated the fundamental dynamic characteristics of magnetically suspended rotors by formulating the AMB dynamics on the basis of rotor-dynamics and vibration theory. Wu et al. [5] proposed an analytical dynamic modeling approach for an active magnetic bearing (AMB)–supported rotor system in a magnetic levitation steam turbine. The flexible rotor is discretized using Euler–Bernoulli beam theory, while the disk–shaft connection is represented by an equivalent spring–damper model with stiffness and damping parameters identified via three-dimensional finite element analysis; the AMB control forces are also incorporated into the model. Narsakka et al. [6] extended conventional analytical methodologies to assess rotor stress and fatigue life under drop-down fault conditions in active magnetic bearing systems. The rotor finite element model, incorporating a nonlinear touchdown bearing contact model, was developed to simulate the dynamic process of rotor descent following levitation loss. Despite superior high-speed

performance, low friction, and controllability relative to mechanical bearings, magnetic bearings face significant thermal challenges in operation. Uneven heat dissipation among windings causes localized heating and thermal imbalance, while temperature gradients during high-speed rotation can induce rotor deformation, known as thermal bowing, degrading system stability and precision [7]. Regarding the thermal and thermo-mechanical behavior of magnetic-bearing–rotor systems, extensive theoretical and experimental studies have been conducted in recent years. Badykov et al. [8] proposed an improved hybrid axial electromagnetic bearing design that effectively reduces power consumption and heat generation, and performed numerical simulations using two-dimensional magnetostatic and two- and three-dimensional thermal finite element analyses. Takahashi et al. [9] attributed the synchronous vibration instability near critical speeds in a magnetic bearing-supported, two-stage overhung centrifugal compressor to the coupling of iron-loss concentration and thermal bending, clarifying its generation mechanism through theoretical modeling. Xu et al. [10] proposed an integrated multi-physics simulation framework that couples electromagnetic, thermal, and mechanical fields, enabling quantitative analysis of cross-scale interactions. This framework provides a systematic approach for investigating thermally induced vibration in magnetically suspended rotors. Jin et al. [11] integrated ANSYS Maxwell with COMSOL to develop a magneto-thermal coupling approach, which was used to analyze the mechanism and parametric influences of iron-loss concentration and the resulting temperature distribution in magnetic bearings, providing a theoretical foundation for addressing related

loss and thermal-imbalance issues. Zhao et al. [12] developed a simplified thermoelastic rotordynamic model by deriving the thermal potential energy under arbitrary temperature fields and establishing the governing equations of motion via the Euler–Lagrange method. Cui et al. [13] established a dynamic model for an axially loaded thin-walled shaft–disk rotor under non-uniform temperature fields, taking into account temperature-dependent material properties, gyroscopic effects, and centrifugal forces. To further investigate nonlinear dynamics and bidirectional thermo-mechanical coupling in rotor systems, Chang et al. [14] derived the equations of motion using the Lagrangian method while accounting for thermally induced variations in bearing radial clearance. A thermal network model, combining lumped-parameter and full-network approaches, was established for the bearing and coupled with the rotor dynamic equations through the bearing mechanical model. In addition, the same research group proposed a thermo-mechanically coupled model for a dual-rotor system, incorporating multiple nonlinear factors as well as heat generation effects in four bearings, thereby enabling comprehensive analysis of nonlinear characteristics under thermo-mechanical coupling conditions [15]. Yu et al. [16] constructed a spatially distributed heating setup to simulate non-uniform thermal environments and conducted experiments on the thermally induced bending deformation and dynamic behavior of an aero-engine high-pressure rotor. The tests systematically measured rotor temperature profiles, structural deformation, and vibration response. Goldman et al. [17] established a quasi-static rotor heat transfer model based on contact heat generation to derive the complex-variable differential equation for thermal bending, investigating its effects along with imbalance and radial loads on intermittent rub-impact vibration. Larsson [18, 19] modeled rotor vibration and journal temperature to analyze unsteady bearing heat transfer, developing a dynamic method for predicting shaft thermal bending vibrations.

Although extensive studies have been conducted on the dynamic modeling of active magnetic bearing (AMB) systems, temperature field analysis, and thermo-mechanical coupling of rotor systems, the dynamic characteristics of rotor systems under the combined effects of AMB heat losses and ambient temperature have not yet been systematically investigated. To address this gap, a thermally coupled rotordynamic model of an AMB-supported rotor system is developed, in which thermally induced loads derived from the temperature field, disk unbalance, gravity, and the equivalent stiffness and damping of the AMB governed by PID control parameters are incorporated. The proposed model is validated by comparison with finite element modal results and with published trends in the equivalent stiffness and damping of AMBs. Based on the developed model, the effects of bias current, rotational speed, and ambient temperature on the system's dynamic response are systematically analyzed. This study provides a theoretical basis for thermal stability assessment and vibration control of AMB-supported rotor systems under high-temperature conditions.

2 METHODS AND MATERIALS

Given the complexity of dynamic modeling for the multiphysics-coupled system, the following assumptions and simplifications are adopted in this study:

1. The AMB rotor is rigidly connected to the shaft–disk system without relative rotation, and is considered an integral part of the shafting system;
2. The rotor operates under thermal steady-state conditions, and the temperature field is therefore assumed to be time-invariant;
3. Only the thermal bending moments about the X and Y axes are considered, and they are treated as quasi-steady excitations in the vibration analysis.

4. The ambient temperature is imposed as an external thermal boundary condition for the AMB-supported rotor system. Thermally induced rotor bending is considered, whereas the temperature-dependent variations in the electromagnetic properties of the AMB materials and the control parameters are neglected.

2.1 Modeling of Shaft and Disk System Dynamics

2.1.1 Shaft Segment

A Timoshenko beam element, shown schematically in Fig. 1, is employed to model individual shaft segments. Each node of the Timoshenko beam element has five degrees of freedom: three translational displacements along the X, Y, and Z axes and two rotational displacements about the X and Y axes. The element therefore has ten generalized coordinates, expressed as follows:

$$\mathbf{u} = [x_a, y_a, z_a, \theta_{xa}, \theta_{ya}, x_b, y_b, z_b, \theta_{xb}, \theta_{yb}]^T. \quad (1)$$

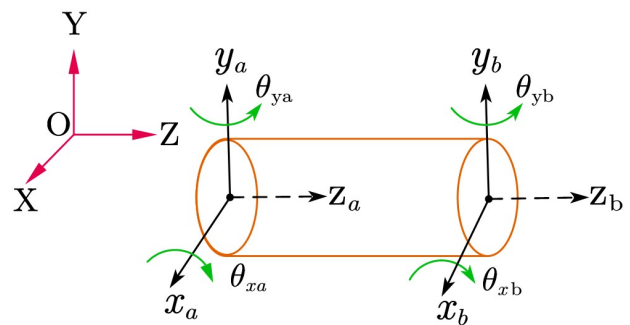


Fig. 1. Timoshenko beam element model

Using Timoshenko beam theory with five degrees of freedom per node, the mass, gyroscopic, and stiffness matrices of the shaft element are denoted by $\mathbf{M}_{all}$, $\mathbf{G}_{all}$, and $\mathbf{K}_{all}$, respectively [20]. Their associated parameters and the formulations of these matrices are provided in the following equations:

$$\Phi = \frac{12EI}{\mu GAL^2}, \quad (2)$$

where Φ denotes the shear factor, E represents the elastic modulus of the shaft material, I indicates the cross-sectional second moment of area of the shaft element, L denotes the length of the shaft element, G represents the shear modulus of the material, A represents the cross-sectional area of the shaft element. The shear correction coefficient μ depends on the shaft geometry. For the solid circular shaft considered in this study, it is calculated as $\frac{7+6\nu}{6(1+\nu)}$, and ν denotes Poisson's ratio of the material.

$$\mathbf{M}_{all} = \mathbf{M}_R + \mathbf{M}_T, \quad (3)$$

$$\mathbf{M}_R = \frac{\rho AL}{(1 + \Phi)^2} \begin{bmatrix} M_{r1} & 0 & 0 & 0 & M_{r4} & M_{r5} & 0 & 0 & 0 & -M_{r6} \\ 0 & M_{r1} & 0 & -M_{r4} & 0 & 0 & M_{r5} & 0 & M_{r6} & 0 \\ 0 & 0 & M_{r3} & 0 & 0 & 0 & 0 & M_{r8} & 0 & 0 \\ 0 & -M_{r4} & 0 & M_{r2} & 0 & 0 & -M_{r6} & 0 & M_{r7} & 0 \\ M_{r4} & 0 & 0 & 0 & M_{r2} & M_{r6} & 0 & 0 & 0 & M_{r7} \\ M_{r5} & 0 & 0 & 0 & M_{r6} & M_{r1} & 0 & 0 & 0 & -M_{r4} \\ 0 & M_{r5} & 0 & -M_{r6} & 0 & 0 & M_{r1} & 0 & M_{r4} & 0 \\ 0 & 0 & M_{r8} & 0 & 0 & 0 & 0 & M_{r3} & 0 & 0 \\ 0 & M_{r6} & 0 & M_{r7} & 0 & 0 & M_{r4} & 0 & M_{r2} & 0 \\ -M_{r6} & 0 & 0 & 0 & M_{r7} & -M_{r4} & 0 & 0 & 0 & M_{r2} \end{bmatrix} \quad (4)$$

$$\begin{aligned} M_{r1} &= \frac{13}{35} + \frac{7}{10}\Phi + \frac{1}{3}\Phi^2, & M_{r2} &= \left(\frac{1}{105} + \frac{1}{60}\Phi + \frac{1}{120}\Phi^2 \right) L^2, \\ M_{r3} &= \frac{1}{3}(1 + \Phi)^2, & M_{r4} &= \left(\frac{11}{210} + \frac{11}{120}\Phi + \frac{1}{24}\Phi^2 \right) L, \\ M_{r5} &= \frac{9}{70} + \frac{3}{10}\Phi + \frac{1}{6}\Phi^2, & M_{r6} &= \left(\frac{13}{420} + \frac{3}{40}\Phi + \frac{1}{24}\Phi^2 \right) L, \\ M_{r7} &= -\left(\frac{1}{140} + \frac{1}{60}\Phi + \frac{1}{120}\Phi^2 \right) L^2, & M_{r8} &= \frac{1}{6}(1 + \Phi)^2. \end{aligned}$$

$$\mathbf{M}_T = \frac{\rho I}{L(1+\Phi)^2} \begin{bmatrix} M_{t1} & 0 & 0 & 0 & M_{t4} & -M_{t1} & 0 & 0 & 0 & M_{t4} \\ 0 & M_{t1} & 0 & -M_{t4} & 0 & 0 & -M_{t1} & 0 & -M_{t4} & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & -M_{t4} & 0 & M_{t2} & 0 & 0 & M_{t4} & 0 & M_{t3} & 0 \\ M_{t4} & 0 & 0 & 0 & M_{t2} & -M_{t4} & 0 & 0 & 0 & M_{t3} \\ -M_{t1} & 0 & 0 & 0 & -M_{t4} & M_{t1} & 0 & 0 & 0 & -M_{t4} \\ 0 & -M_{t1} & 0 & M_{t4} & 0 & 0 & M_{t1} & 0 & M_{t4} & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & -M_{t4} & 0 & M_{t3} & 0 & 0 & M_{t4} & 0 & M_{t2} & 0 \\ M_{t4} & 0 & 0 & 0 & M_{t3} & -M_{t4} & 0 & 0 & 0 & M_{t2} \end{bmatrix} \quad (5)$$

$$M_{t1} = \frac{6}{5}, \quad M_{t2} = \left(\frac{2}{15} + \frac{1}{6}\Phi + \frac{1}{3}\Phi^2 \right) L^2, \\ M_{t3} = -\left(\frac{1}{30} + \frac{1}{6}\Phi - \frac{1}{6}\Phi^2 \right) L^2, \quad M_{t4} = \left(\frac{1}{10} - \frac{1}{2}\Phi \right) L.$$

$$\mathbf{G}_{all} = \frac{\rho I}{15L(1+\Phi)^2} \begin{bmatrix} 0 & -G_1 & 0 & G_2 & 0 & 0 & G_1 & 0 & G_2 & 0 \\ G_1 & 0 & 0 & 0 & G_2 & -G_1 & 0 & 0 & 0 & G_2 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ -G_2 & 0 & 0 & 0 & -G_4 & G_2 & 0 & 0 & 0 & G_3 \\ 0 & -G_2 & 0 & G_4 & 0 & 0 & G_2 & 0 & -G_3 & 0 \\ 0 & G_1 & 0 & -G_2 & 0 & 0 & -G_1 & 0 & -G_2 & 0 \\ -G_1 & 0 & 0 & 0 & -G_2 & G_1 & 0 & 0 & 0 & -G_2 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ -G_2 & 0 & 0 & 0 & G_3 & G_2 & 0 & 0 & 0 & -G_4 \\ 0 & -G_2 & 0 & -G_3 & 0 & 0 & G_2 & 0 & G_4 & 0 \end{bmatrix} \quad (6)$$

$$G_1 = 36, \quad G_2 = (3 - 15\Phi)L, \\ G_3 = (1 + 5\Phi - 5\Phi^2)L^2, \quad G_4 = (4 + 5\Phi + 10\Phi^2)L^2.$$

$$\mathbf{K}_{all} = \frac{EI}{(1+\Phi)L^3} \begin{bmatrix} K_1 & 0 & 0 & 0 & K_4 & -K_1 & 0 & 0 & 0 & K_4 \\ 0 & K_1 & 0 & -K_4 & 0 & 0 & -K_1 & 0 & -K_4 & 0 \\ 0 & 0 & K_3 & 0 & 0 & 0 & 0 & -K_3 & 0 & 0 \\ 0 & -K_4 & 0 & K_2 & 0 & 0 & K_4 & 0 & K_5 & 0 \\ K_4 & 0 & 0 & 0 & K_2 & -K_4 & 0 & 0 & 0 & K_5 \\ -K_1 & 0 & 0 & 0 & -K_4 & K_1 & 0 & 0 & 0 & -K_4 \\ 0 & -K_1 & 0 & K_4 & 0 & 0 & K_1 & 0 & K_4 & 0 \\ 0 & 0 & -K_3 & 0 & 0 & 0 & 0 & K_3 & 0 & 0 \\ 0 & -K_4 & 0 & K_5 & 0 & 0 & K_4 & 0 & K_2 & 0 \\ K_4 & 0 & 0 & 0 & K_5 & -K_4 & 0 & 0 & 0 & K_2 \end{bmatrix} \quad (7)$$

$$K_1 = 12, \quad K_2 = (4 + \Phi)L^2, \\ K_3 = \frac{A}{I}(1 + \Phi)L^2, \quad K_4 = 6L, \\ K_5 = (2 - \Phi)L^2.$$

In Equations (5–7), ρ denotes the material density, and the remaining parameters are defined in Eq. (2).

Furthermore, the model incorporates the influence of the shafting's own weight, which is expressed in the dynamic formulation as:

$$\mathbf{G}_{sw} = G_w L g \begin{bmatrix} 0 & -\frac{1}{2} & \frac{L}{12} & 0 & 0 & 0 & -\frac{1}{2} & -\frac{L}{12} & 0 & 0 \end{bmatrix}^T, \quad (8)$$

where G_w denotes the linear mass density (mass per unit length), g is the gravitational acceleration, and L has the same meaning as in Eq. (2).

2.1.2 Disk Element

The disk is modeled as a rigid finite element whose axis of rotation passes through its center of mass. The mass matrix $\mathbf{M}_{disk}$ and the gyroscopic matrix $\mathbf{G}_{disk}$ generated by the disk element can be represented by the following matrices, where m_d is the mass of the disk element, J_d and J_p denote the diametral and polar mass moments of

inertia, respectively.

$$\mathbf{M}_{disk} = \begin{bmatrix} m_d & 0 & 0 & 0 & 0 \\ 0 & m_d & 0 & 0 & 0 \\ 0 & 0 & m_d & 0 & 0 \\ 0 & 0 & 0 & J_d & 0 \\ 0 & 0 & 0 & 0 & J_d \end{bmatrix}, \quad (9)$$

$$\mathbf{G}_{disk} = \begin{bmatrix} 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & J_p \\ 0 & 0 & 0 & -J_p & 0 \end{bmatrix}.$$

2.2 AMB Equivalent Stiffness and Damping Model

In this study, an 8-pole active magnetic bearing is selected as the support for the rotor system, and its schematic structure is illustrated in Fig. 2, in which each magnetic pole and corresponding region is clearly labeled.

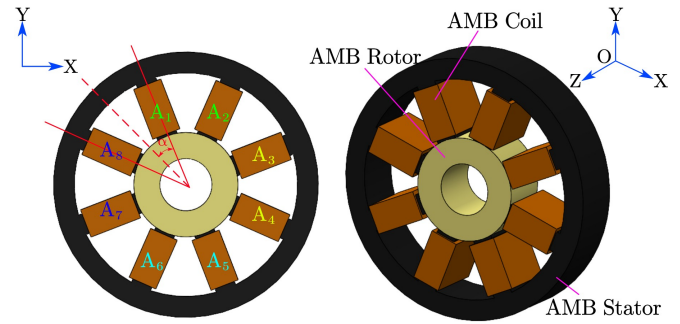


Fig. 2. Schematic diagram of the active magnetic bearing structure

In this work, the active magnetic bearing (AMB) is modeled in the rotordynamic formulation as equivalent stiffness and damping elements obtained from linearization of the closed-loop system with fixed PID gains. Electromagnetic nonlinearities and temperature-dependent parameter variations are disregarded within the considered operating range. As a result, the equivalent stiffness and damping are not constants but quantities that vary with rotational frequency. The relevant formulas and dynamic matrices required for the calculations are provided below [21].

The expressions for the displacement stiffness (k_x) and the current stiffness (k_i) are given by:

$$\begin{cases} k_x = -\frac{\mu_0 A_b N^2 I_b^2 \cos(\alpha)}{\delta_0^3} \\ k_i = \frac{\mu_0 A_b N^2 I_b \cos(\alpha)}{\delta_0^2} \end{cases}, \quad (10)$$

where μ_0 is the permeability of free space, A_b represents the area of the magnetic poles, N is the number of coil turns, I_b denotes the bias current, δ_0 represents the nominal air gap length, and α corresponds to half of the inter-pole angle.

The formulas for calculating the equivalent stiffness and damping of the active magnetic bearing, considering the influence of PID parameters, are given by:

$$\begin{cases} K_{amb} = k_x + k_i \operatorname{Re} \left\{ P_1 P_2 P_3 \left(k_p + \frac{k_{ic}}{s} + \frac{k_d s}{1 + T_0 s} \right) \left(\frac{1}{b_s + 1} \right) \left(\frac{(1 - a T_s)^2}{(1 + a T_s)^2} \right) \right\}, \\ C_{amb} = \frac{k_i}{\omega} \operatorname{Im} \left\{ P_1 P_2 P_3 \left(k_p + \frac{k_i}{s} + \frac{k_d s}{1 + T_0 s} \right) \left(\frac{1}{b_s + 1} \right) \left(\frac{(1 - a T_s)^2}{(1 + a T_s)^2} \right) \right\}. \end{cases} \quad (11)$$

where P_1 , P_2 , and P_3 are the gain coefficients of the sensor, power amplifier, and controller, respectively; k_p , k_{ic} , k_d , and T_0 denote the PID controller parameters; b_s represents the parameter used in the

calculation of the power amplifier; a is the coefficient of the controller model; ω denotes the rotational speed; and T_s denotes the time delay.

In the dynamic modeling framework, the active magnetic bearing is expressed in matrix form as:

$$\mathbf{K}_{AMB} = \begin{bmatrix} K_{amb} & 0 & 0 & 0 & 0 \\ 0 & K_{amb} & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 \end{bmatrix}, \quad (12)$$

$$\mathbf{C}_{AMB} = \begin{bmatrix} C_{amb} & 0 & 0 & 0 & 0 \\ 0 & C_{amb} & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 \end{bmatrix}.$$

2.3 Modeling Additional Loads in AMB-Rotor Systems

In this study, the rotating unbalance forces of the disk and the thermally induced bending loads of the rotor (resulting from the combined effects of ambient temperature and heat losses in the active magnetic bearing coils) are incorporated as additional forces and moments in the AMB-rotor system.

1. The expressions for the unbalance forces ($\mathbf{Q}_u$) of the disk in the X and Y directions are given as:

$$\begin{cases} Q_{ux} = m_d e_d \omega^2 \cos(\omega t + \varphi) \\ Q_{uy} = m_d e_d \omega^2 \sin(\omega t + \varphi) \end{cases}, \quad (13)$$

where m_d is the disk mass, e_d is the disk eccentricity, and ω is the rotational angular speed.

2. To determine the thermally induced bending moments under realistic thermal conditions, a three-dimensional steady-state thermal analysis is first performed using finite-element software to obtain the temperature field of the AMB-rotor system. The corresponding thermal stress distribution at each nodal cross-section is subsequently obtained through thermal stress analysis. At a given cross-section, the axial thermal stress σ_z acting on an infinitesimal area dA_s produces an elemental axial force $dF_z = \sigma_z dA_s$. With b_x and b_y denoting the signed moment arms from the area element to the X and Y axes, respectively, the corresponding elemental bending moments are expressed as follows [17]:

$$\begin{cases} dM_x = b_x dF_z \\ dM_y = b_y dF_z \end{cases}. \quad (14)$$

Integrating these elemental moments over the entire cross-sectional area gives the sectional thermal bending moments M_x and M_y , as expressed in Eq. (15).

$$\begin{cases} M_x = \int_{A_s} \sigma_z b_x dA_s \\ M_y = \int_{A_s} \sigma_z b_y dA_s \end{cases}. \quad (15)$$

The thermal bending moment values at each nodal cross-section in the rotordynamic model are computed using Eq. (16).

$$\begin{cases} M'_x = M'_y = 0 \\ M'_x(n) = M_x(n-1) - M_x(n) \\ M'_y(n) = M_y(n-1) - M_y(n) \end{cases}, \quad (16)$$

where n denotes the index of the nodal cross-section along the axial direction of the rotor, which is consistent with the node numbering used in the rotor dynamic model. The resulting equivalent nodal moments are assembled into the global thermal-load vector at the rotational degrees of freedom θ_x and θ_y , thereby forming the thermally induced load vector ($\mathbf{Q}_{thermal}$).

2.4 Thermally Coupled Dynamic Equations of the AMB-Rotor System

Based on the descriptions provided in Subsections 2.1 to 2.3 and the associated assumptions, together with the rotor-dynamic system modeling principles, the governing equations are first expressed in matrix form for each subsystem and then consolidated into a unified differential equation representing the magnetically suspended rotor system subjected to prescribed thermally induced loads. The resulting governing equation is given by Eq. 17 as follows:

$$(\mathbf{M}_{all} + \mathbf{M}_{disk})\ddot{\mathbf{X}} + (\mathbf{C} - \omega(\mathbf{G}_{all} + \mathbf{G}_{disk}) + \mathbf{C}_{AMB})\dot{\mathbf{X}} + (\mathbf{K}_{all} + \mathbf{K}_{AMB})\mathbf{X} = \mathbf{Q}_{weight} + \mathbf{Q}_{thermal} + \mathbf{Q}_u. \quad (17)$$

Here, $\mathbf{C}$ is the proportional damping matrix and is expressed as $\mathbf{C} = \eta(\mathbf{M}_{all} + \mathbf{M}_{disk}) + \beta(\mathbf{K}_{all} + \mathbf{K}_{AMB})$. The coefficient η is calculated by $\eta = 2 \left(\frac{\xi_2}{\omega_2} - \frac{\xi_1}{\omega_1} \right) / \left(\frac{1}{\omega_2^2} - \frac{1}{\omega_1^2} \right)$, and the coefficient β is determined by $\beta = \frac{2(\xi_2 \omega_2 - \xi_1 \omega_1)}{\omega_2^2 - \omega_1^2}$, where $\xi_{1,2}$ denote the first two damping ratios of the system respectively, while $\omega_{1,2}$ represent the first two natural frequencies of the system. On the other hand, the matrices $\mathbf{Q}_{weight}$, $\mathbf{Q}_{thermal}$ and $\mathbf{Q}_u$ represent the total gravitational load of the shaft-disk assembly, the distributed equivalent thermal bending moments at the nodal shaft cross-sections and the disk-induced unbalance forces, respectively. Meanwhile, $\ddot{\mathbf{X}}$, $\dot{\mathbf{X}}$, and $\mathbf{X}$ represent the acceleration, velocity, and displacement vectors, respectively. The time-domain response of Eq. (17) is obtained using the Newmark- β method with the constant-average-acceleration scheme, for which $\gamma = 0.5$ and $\beta = 0.25$. The time step is determined as $2\pi/(1024\omega)$.

2.5 Finite Element Calculation of Thermally Induced Bending Moments

A three-dimensional finite element model of the AMB-supported rotor system is constructed using the actual structural dimensions and then preprocessed in the finite element software. The three-dimensional analysis consists of a steady-state thermal analysis followed by thermal-stress analysis. The material properties of the shaft, AMB rotor, stator, and coils are defined accordingly. In particular, the temperature dependence of the shaft properties, including Young's modulus and Poisson's ratio, is taken into account. Since the present study focuses on the rotor dynamic response to thermal loading, the temperature dependence of the material properties of the remaining AMB components is neglected. Thermal boundary conditions, including coil heat generation, convective heat transfer coefficients, and ambient temperature, are then applied. The model is discretized using an automatic meshing scheme, with an element size of 4.5 mm for the shaft and 4 mm for the remaining components, as shown in Fig. 3.

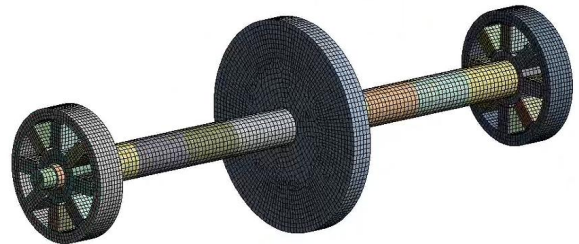


Fig. 3. Finite element mesh model of the active magnetic bearing rotor system

After the steady-state thermal analysis is completed, the three-dimensional temperature field distributions under different ambient temperatures are obtained, as shown in Fig. 4. Based on the obtained temperature field, the corresponding thermal stress distribution at each rotor nodal cross-section is derived through thermal-stress

analysis. Furthermore, based on the thermal stress results derived from the finite element temperature field, the equivalent thermal bending moments between adjacent nodal cross-sections are calculated and extracted according to Eqs. (14-16). These equivalent thermal bending moments are subsequently assembled into the thermal load vector Q_{thermal} and included in the governing rotordynamic equation.

Table 1. Parameters of the Thermally Coupled AMB-Rotor System

Parameter	Symbol	Value
Number of rotor nodes	N_{node}	16
Length of each shaft segment (m)	L_1	1.5×10^{-2}
	L_2	8×10^{-3}
	L_3	6×10^{-2}
	L_4	7×10^{-2}
	L_5	2×10^{-2}
	L_6	2.7×10^{-2}
Outer diameter of each shaft section (m)	$D_1(L_1)$	2×10^{-2}
	$D_2(L_2)$	2.5×10^{-2}
	$D_3(L_3, L_4)$	3.5×10^{-2}
	$D_4(L_5)$	3×10^{-2}
	$D_5(L_6)$	5×10^{-2}
Young's modulus of the shaft (20°C) (GPa)	E	200
Material density of shaft and AMB rotor (kg/m ³)	ρ	7850
Poisson's ratio of the shaft and AMB rotor (20°C)	ν	0.3
Disk mass (kg)	m_d	4.8
Disk diametral mass moment of inertia (kg·m ²)	J_d	1.25×10^{-2}
Disk polar moment of inertia (kg·m ²)	J_p	2.5×10^{-2}
Eccentricity of the disk (m)	e_d	5×10^{-5}
Permeability of free space	μ_0	1.3×10^{-6}
Magnetic-pole area (m ²)	A_b	2.6×10^{-4}
Number of turns per coil	N	160
Half-angle between the pole legs of the AMB (°)	α	22.5
The nominal air gap length of AMB (m)	δ_0	3×10^{-4}
Sensor gain coefficient	P_1	1.6×10^4
Power-amplifier gain coefficient	P_2	1
Controller coefficient	P_3	4
PID controller parameters	k_p	0.6
	k_{ic}	30
	k_d	2×10^{-3}
	T_0	1×10^{-4}
	g	10
Gravitational acceleration (m/s ²)		
Thermal loss dissipation of AMB at A_1, A_2 (W/m ³)	W_{A1}, W_{A2}	4.1×10^6
Volumetric heat-generation rate A_3 - A_8 (W/m ³)	W_{A3} - W_{A8}	1.65×10^5
Air convection heat transfer coefficient (W/m ² ·°C)	Air_c	15
Overall heat-transfer coefficient of the coil (W/m ² ·°C)	$Coil_c$	13.3
Overall heat-transfer coefficient of the rotor (W/m ² ·°C)	$Rotor_c$	14
Overall heat-transfer coefficient of the stator (W/m ² ·°C)	$Stator_c$	16.7
Density of the coil material (kg/m ³)	ρ_{coil}	8960
Density of the stator material (kg/m ³)	ρ_{stator}	7650
Thermal conductivity of the coil material (W/m·°C)	$Coil_T$	400
Thermal conductivity of stator and rotor (W/m·°C)	$Rotor_T, Stator_T$	35
Specific heat capacity of the coil material (J/kg·°C)	$Coil_s$	385
Specific heat capacity of the stator and rotor materials (J/kg·°C)	$Rotor_s, Stator_s$	450

2.6 Model Parameters and Analysis Procedure

This section outlines the model parameters, thermal boundary conditions, and research procedure. The system schematic and overall research flowchart are shown in Figs. 5 and 6, respectively.

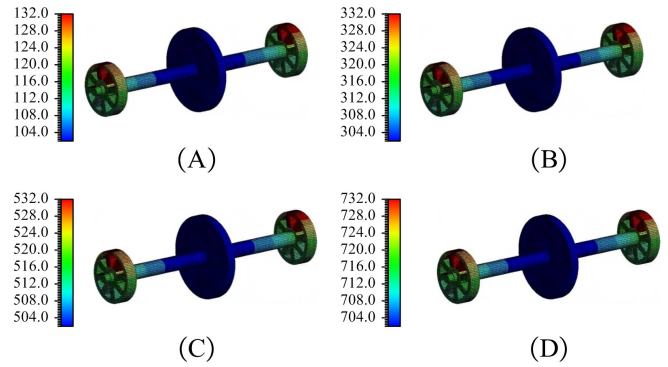


Fig. 4. Steady-state temperature distributions of the AMB-supported rotor system under different ambient temperatures (A: 100°C; B: 300°C; C: 500°C; D: 700°C)

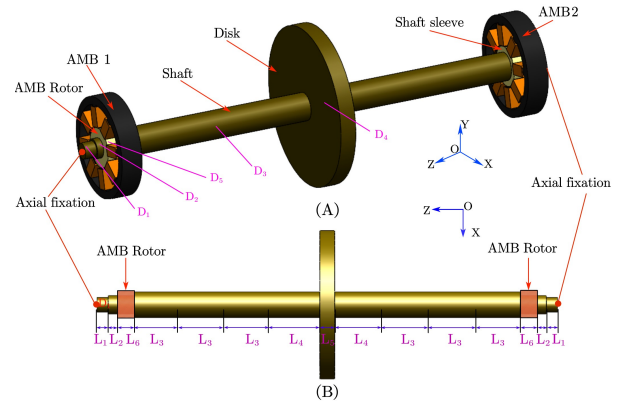


Fig. 5. Schematic of the AMB-rotor system: A three-dimensional configuration; B rotor-node discretization

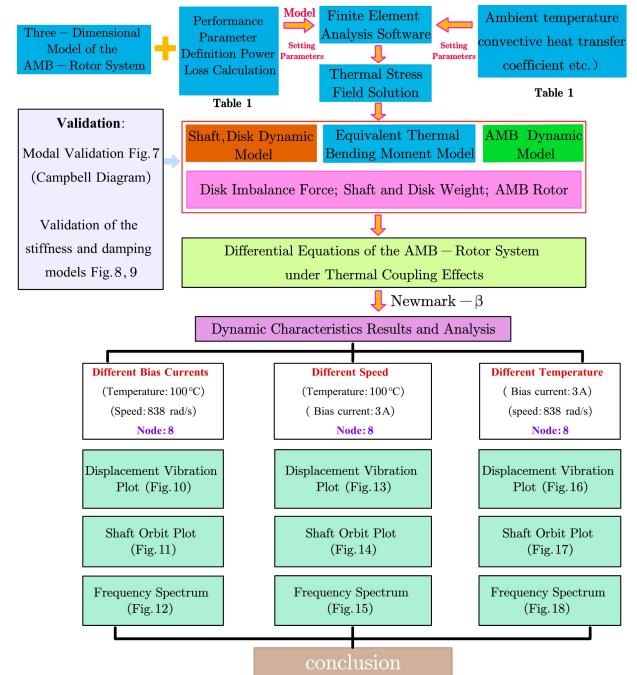


Fig. 6. Research and analysis workflow

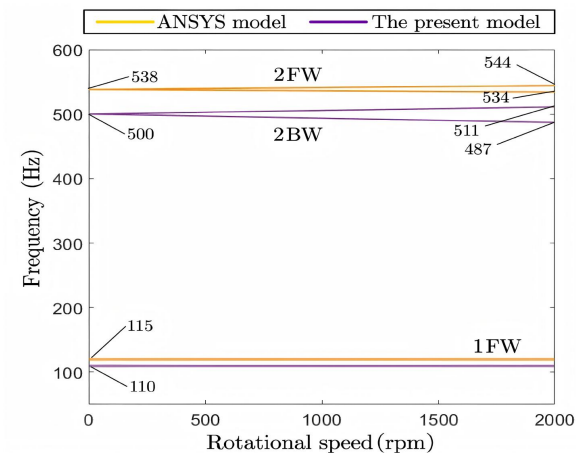
The model parameters used in this study are summarized in Table 1. The overall analysis procedure is illustrated in the workflow shown

in Fig. 6. Additionally, this study validates the rotor dynamics model and the equivalent stiffness-damping model of the active magnetic bearings, solves the dynamic model using the Newmark- β method, and analyzes the thermally coupled dynamic characteristics of the AMB-supported rotor system. The validation results and parametric analyses are presented in the following section.

3 VALIDATION

To assess the basic accuracy of the developed rotordynamic model, a modal validation is first performed. Since the construction of the proportional damping matrix requires the first two modal frequencies, the modal frequencies predicted by the present model are compared with those obtained from the ANSYS finite element model over a rotational speed range of 0–2000 rpm. The comparison results are shown in Fig. 7. The first two modal frequencies predicted by the present model show good agreement with the finite element results in both magnitude and trend, and the maximum relative error of the modal frequencies is 8.8%. These results support the basic reliability of the developed rotordynamic model and provide a reasonable basis for the subsequent dynamic analyses.

To assess the validity of the equivalent stiffness and damping model used in this study, their variations with rotational frequency were calculated and compared with those reported in [22], as shown in Fig. 8. Since the bearing structural parameters and control parameters used in this study are not identical to those in [22], this comparison is mainly intended for qualitative trend validation.



Rotational speed (rpm)	Mode order	Present model (Hz)	ANSYS model (Hz)	Relative error (%)
0	First-order natural frequency	110	115	4.4%
2000	First-order natural frequency	110	115	4.4%
0	Second-order natural frequency	500	538	7.1%
2000	Second-order natural frequency (FW)	487	534	8.8%
2000	Second-order natural frequency (BW)	511	544	6.1%

Fig. 7. Comparison of Campbell diagrams obtained from the present and ANSYS models: FW forward, BW backward

The overall trends predicted by the present model are consistent with the published results. The variation in the equivalent stiffness and

damping can be explained as follows. The equivalent stiffness is jointly determined by the displacement stiffness term and the real part of the feedback current stiffness term. Since the displacement stiffness term is negative and the feedback current stiffness term varies with rotational frequency, the equivalent stiffness first increases and then decreases as the rotational frequency increases, and may become negative at higher frequencies. The equivalent damping is mainly governed by the imaginary part of the feedback control term and the rotational frequency. In the low-frequency range, the integral term of the PID controller may lead to negative equivalent damping. As the rotational frequency increases, the equivalent damping rapidly changes from negative to positive. With a further increase in rotational frequency, the system time-delay effect becomes more pronounced, leading to a gradual decrease in the equivalent damping, which eventually approaches zero.

Furthermore, a mesh-sensitivity analysis is performed to assess the dependence of the finite element temperature predictions on the shaft mesh size. A representative high-temperature condition with an ambient temperature of 100 °C is considered, while all other boundary conditions and the mesh settings of the remaining components are kept unchanged. The shaft mesh sizes are set to 2.5, 3.5, 4.5, 5.5, and 6.5 mm, and the corresponding average shaft temperature is calculated for each mesh. Using the result obtained with the 4.5 mm mesh as the baseline, the relative deviation of each result from the baseline value is evaluated, as shown in Fig. 9.

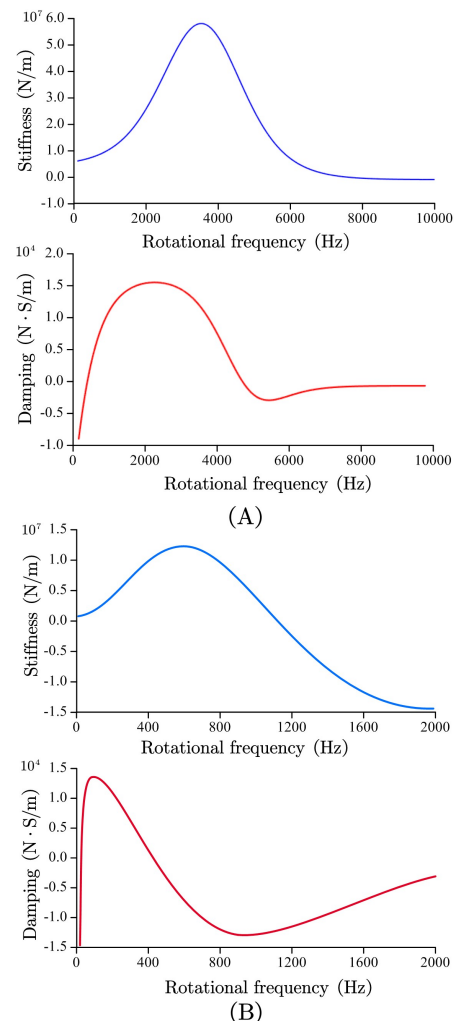


Fig. 8. Equivalent stiffness and damping of the AMB as functions of rotational frequency (A present model; B the model from the literature [22])

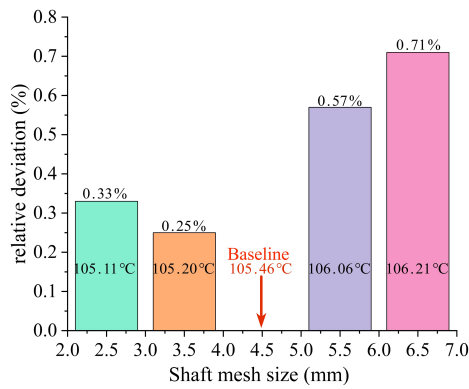


Fig. 9. Relative deviations in the average shaft temperature for different mesh sizes (4.5 mm baseline)

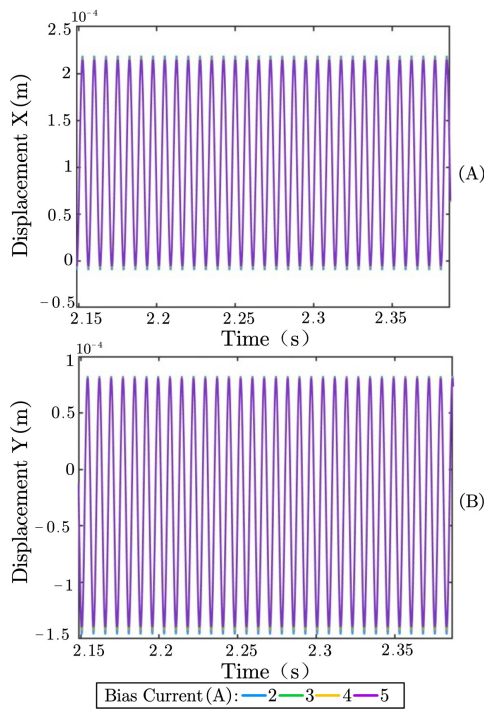


Fig. 10. Displacement responses in X and Y directions at different bias currents. (A: X-direction; B: Y-direction)

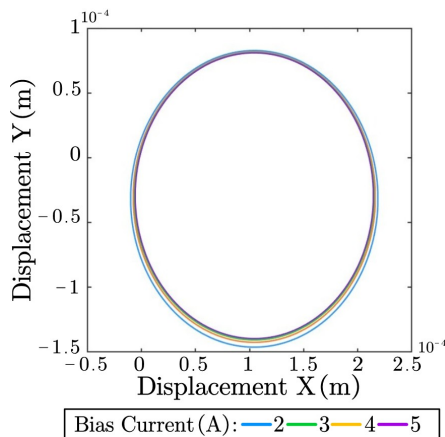


Fig. 11. Shaft orbit plot at different bias currents

When the shaft mesh is further refined from 4.5 mm to 3.5 and 2.5 mm, the relative deviations in the average shaft temperature are only 0.25 % and 0.33 %, respectively. These results indicate that the predicted average shaft temperature is insensitive to further mesh refinement below 4.5 mm. Therefore, a shaft mesh size of 4.5 mm is adopted in the subsequent finite element analyses.

4 DISCUSSION

This section examines the effects of bias current, rotational speed, and ambient temperature on the dynamic response of the AMB-supported rotor system. The study focuses on three key aspects: first, the influence of different bias currents on the dynamic behavior of the system under fixed rotational speed and temperature field conditions; second, the effect of varying rotational speeds on the dynamic response of the system under fixed bias current and temperature field; and third, the impact of different ambient temperatures on the dynamic characteristics of the system under fixed bias current and rotational speed. The rotor disk node (Node 8) is selected as the key observation point. Its dynamic behavior under various operating conditions is analyzed using displacement–time history plots, shaft orbit, and frequency spectrum response diagrams.

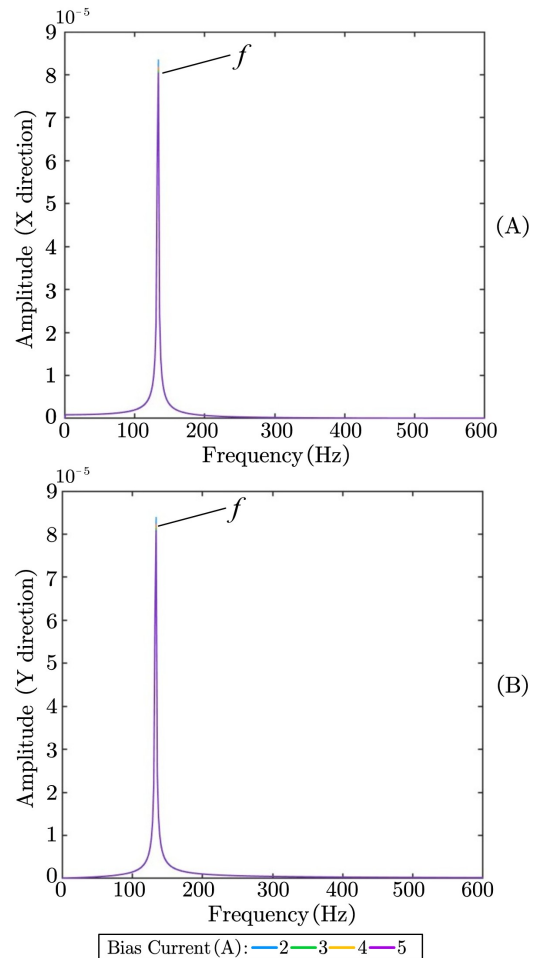


Fig. 12. Frequency spectra in the X and Y directions at different bias currents. (A: X-direction; B: Y-direction)

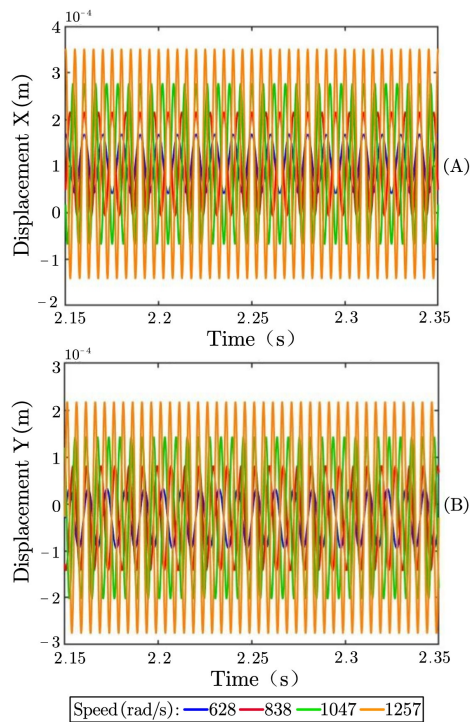


Fig. 13. Displacement responses in X and Y directions at different speeds. (A: X-direction; B: Y-direction)

4.1 Effect of Bias Current on System Dynamics

To investigate the influence of different bias currents on the dynamic characteristics of the system, a baseline operating condition is set with an ambient temperature of 100 °C and a rotational speed of 838 rad/s.

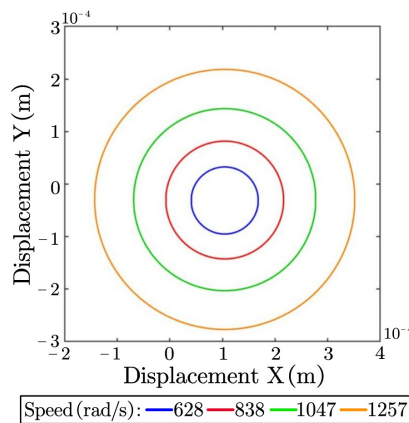


Fig. 14. Shaft orbit plot at different speeds

Figures 10–12 indicate that increasing the bias current leads to a moderate reduction in the displacement amplitude and a contraction of the shaft orbit, while the response remains dominated by the fundamental frequency component ($1f$). Neither additional harmonic components nor changes in the motion period are observed. This indicates that the bias current mainly regulates the response magnitude through the support characteristics of the AMB, rather than altering the frequency composition or motion pattern of the rotor system.

4.2 Effect of Rotational Speed on System Dynamics

To investigate the influence of rotational speed on the dynamic characteristics of the system, the bias current is fixed at 3 A and the ambient temperature is set to 100 °C as the baseline operating condition.

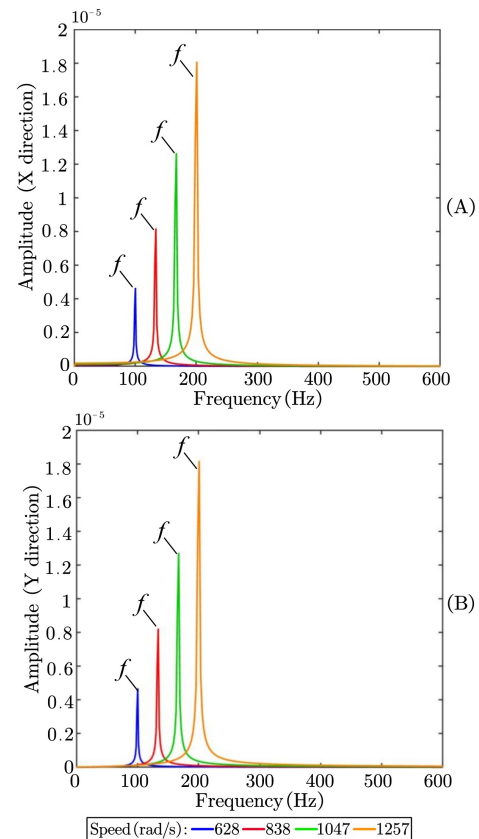


Fig. 15. Frequency spectra in the X and Y directions at different speeds. (A: X-direction; B: Y-direction)

Figures 13–15 show that rotational speed primarily governs the synchronous vibration component. As the rotational speed increases, both the amplitude of the fundamental ($1f$) response and the size of the shaft orbit increase. In particular, the response increases more markedly between 1047 rad/s and 1257 rad/s, indicating enhanced sensitivity near the upper end of the investigated speed range. This behavior results from the combined effects of the speed-dependent unbalance excitation and the gyroscopic matrix term in the governing equations, which jointly influence the vibration response at the system nodes. Nevertheless, the system retains a single-periodic motion throughout the investigated speed range. As the rotational speed increases, the fundamental-frequency peaks in both the X and Y directions shift to higher frequencies and continue to track the corresponding rotational frequency.

4.3 Effect of Ambient Temperature on System Dynamics

To investigate the influence of different ambient temperatures on the dynamic characteristics of the system, the rotational speed is fixed at 838 rad/s and the bias current is set to 3 A.

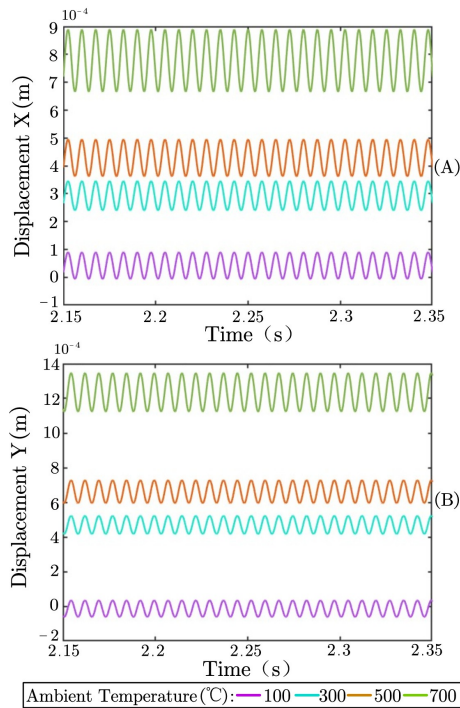


Fig. 16. Displacement responses in X and Y directions at different ambient temperatures. (A: X-direction; B: Y-direction)

Figures 16–18 show that the predominant effect of increasing ambient temperature is a pronounced migration of the shaft-orbit center, rather than the emergence of additional frequency components. As the ambient temperature increases, the mean displacement offsets in both directions increase markedly, and the shaft-orbit center shifts toward the upper-right region. Meanwhile, the system response remains dominated by the synchronous fundamental frequency and retains a single-periodic motion pattern. These observations indicate that the thermally induced bending moments act primarily as quasi-steady loads. As the ambient temperature increases, the overall temperature of the rotor system rises, thereby increasing the bending moments generated by the nonuniform temperature field and causing pronounced changes in the dynamic response.

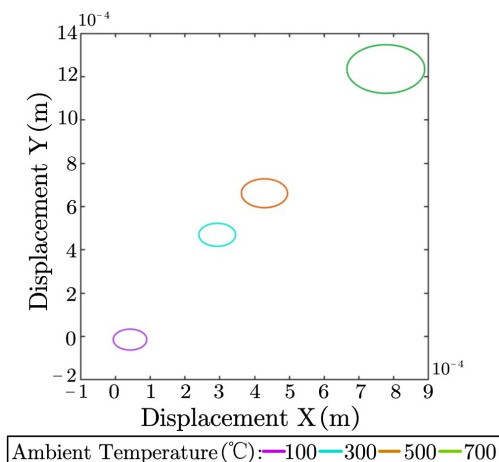


Fig. 17. Shaft orbit plot at different ambient temperatures

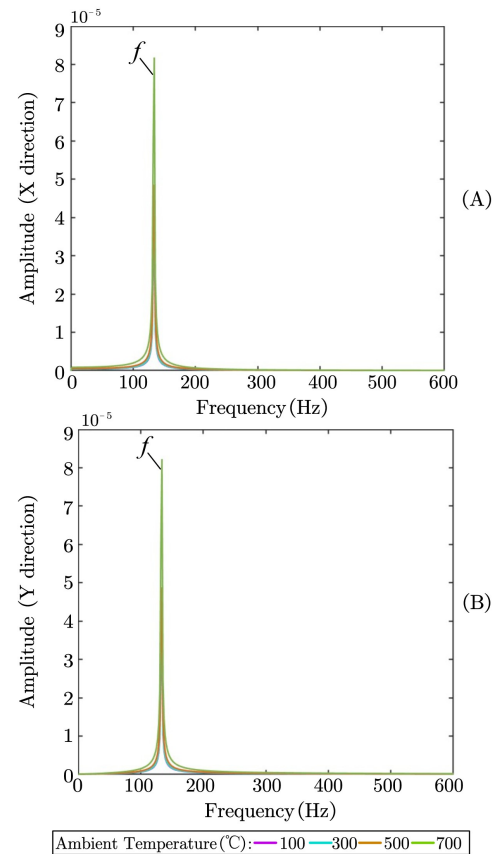


Fig. 18. Frequency spectra in the X and Y directions at different ambient temperatures. (A: X-direction; B: Y-direction)

5 CONCLUSIONS

This study focuses on the thermally induced dynamic behavior of an active magnetic bearing (AMB)-supported rotor system operating under high-temperature conditions. A one-way sequential thermal-mechanical-rotordynamic analysis framework is established by considering the combined effects of AMB heat generation and ambient thermal loading. The model incorporates thermally induced loads derived from the temperature field, disk mass unbalance, gravity, and the equivalent support stiffness and damping of the AMB governed by PID control parameters. Based on the developed model, the dynamic response characteristics of the system under varying bias currents, rotational speeds, and ambient temperatures are systematically investigated. The main conclusions are summarized as follows:

1. Increasing the bias current alters the effective support characteristics of the active magnetic bearing and reduces the displacement amplitude and gradually contracts the shaft orbit. Nevertheless, the spectral content of the response and its single-periodic motion pattern remain essentially unchanged, indicating that the bias current mainly regulates the response magnitude without altering the spectral composition or response periodicity.

2. Rotational speed plays a dominant role in governing the synchronous vibration response. As the speed increases, both the response amplitude and the spatial extent of the shaft orbit increase progressively. The more pronounced growth observed between 1047 rad/s and 1257 rad/s further indicates enhanced response sensitivity in the upper portion of the investigated speed range.

3. Ambient temperature predominantly influences the displacement response and the location of the shaft-orbit center, while its effect

on the spectral composition remains comparatively limited. The pronounced shaft-orbit center migration is mainly associated with the thermal bending moments induced by the temperature field. Throughout the investigated temperature range, the rotor maintains a single-periodic motion state, with the response consistently dominated by the fundamental frequency.

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Data availability The datasets generated and analyzed during the current study are not publicly available because they contain sensitive information, but they are available from the corresponding author upon reasonable request.

Author contribution Peixun Tang: Methodology, Formal analysis, Investigation, Data curation, Writing—original draft, Writing—review and editing; Guilin Li: Methodology, Writing—original draft, Project administration; Zhengminqing Li: Methodology, Investigation, Project administration; Qihang Chen: Writing—original draft. All authors have read and agreed to the published version of the manuscript.

Conflict of interest The authors declare no conflicts of interest.

Ethics approval Ethical approval was not required for this study as it solely involved theoretical analysis/numerical simulations on mechanical components and did not involve human participants, human data, or animal subjects.

Toplotno inducirana dinamika sistema rotorja z aktivnimi magnetnimi ležaji v letalskem motorju

Povzetek Pri visokotemperaturnih obratovalnih pogojih v letalskih motorjih lahko kombinirani vplivi neenakomernega nastajanja toplote v tuljavah aktivnih magnetnih ležajev (AMB) in toplotnih obremenitev okolice povzročijo neenakomerno porazdelitev temperature v rotorskem sistemu, s čimer nastanejo toplotno inducirane upogibne obremenitve, ki poslabšajo dinamično stabilnost sistema. Za obravnavo tega problema je bil razvit termo-mehanski analitični model za rotorski sistem, podprt z AMB. Model vključuje toplotno inducirane obremenitve, izpeljane iz temperaturnega polja, neuravnoteženost diska, gravitacijo ter od PID-regulatorja odvisno ekvivalentno togost in dušenje aktivnih magnetnih ležajev. Vodilne enačbe so rešene z metodo Newmark-β. Na podlagi predlaganega modela so bile sistematično raziskane značilnosti dinamičnega odziva sistema pri različnih predmagnetilnih tokovih, vrtilnih hitrostih in temperaturah okolice. Rezultati kažejo, da pri danih toplotnih pogojih povečanje predmagnetilnega toka izboljša učinkovito podporno sposobnost AMB in s tem zmanjša vibracijski odziv. Nasprotno pa povečanje vrtilne hitrosti postopoma povečuje sinhroni vibracijski odziv, pri čemer je povečanje izrazitejše v zgornjem delu obravnavanega območja vrtilnih hitrosti. Poleg tega zvišanje temperature okolice bistveno poveča toplotno inducirano upogibno vzbujanje, kar povzroči večje amplitude vibracij. To kaže, da v obravnavanem območju obratovanja toplotni učinki močno vplivajo na dinamično obnašanje sistema. Raziskava zagotavlja teoretično osnovo za ocenjevanje toplotne stabilnosti in nadzor vibracij rotorskih sistemov, podprtih z aktivnimi magnetnimi ležaji, pri visokotemperaturnih obratovalnih pogojih.

Ključne besede toplotno inducirane vibracije, aktivni magnetni ležaji, letalski motor, dinamika rotorjev